

LS-53(CANL)  
8/5/85  
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Optimization of  $\beta$  Functions through Insertion Devices

Introduction

It is generally noted that at an undulator straight section, the horizontal beta function is made to be large while the vertical beta function is relatively small. On the other hand, at a wiggler straight section, both horizontal and vertical beta functions are made to be small. In this note we describe a procedure with which optimum settings of the beta functions in the insertion straight section are to be determined. For this we consider separately for the undulator radiation and the radiation from the wiggler device.

Since the brilliance of radiation is a canonically conserved quantity, we use the brilliance as a figure of merit for the consideration. Then the optimization process is to find a set of horizontal and vertical beta functions which would give the maximum brilliance when the natural emittance, emittance coupling constant, length of insertion device and the photon energy to which the insertion device is optimized are specified. The next step of the study is to find sensitivities of the beta functions to the brilliance.

After having done these, we will attempt to find a set of universally optimized beta functions with which all of given kind of the insertion device, e.g., all undulators or all wigglers can be operated. The purpose of this attempt is that if all undulators, regardless of photon energies for which these are optimized, can have the same beta functions, the machine lattice becomes quite simpler and can maintain higher periodicity.

In order to make the description of this study complete, we review some of definitions used herein.

Coupling Constant k: Coupling constant is defined to be

$$\begin{aligned}\epsilon_x &= \epsilon_{x_0} / \sqrt{1 + k} \\ \epsilon_y &= k \epsilon_{x_0} / \sqrt{1 + k}\end{aligned}$$

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where  $\epsilon_{x0}$  is the natural emittance of the storage ring, and  $\epsilon_x$  and  $\epsilon_y$  are the resultant horizontal and vertical emittances due to the coupling of  $k$ , respectively.

Photon flux is defined as number of photons/sec/eV of photon or number of photons/sec/0.1% BW.

Brightness or spectral brightness is defined as

$$\text{Brightness} = \text{Photon flux/apparent source rms solid angle}$$

$$\text{number of photons/sec} \\ = \frac{\text{number of photons/sec}}{\Omega \text{ (0.1% BW)}}$$

where  $\Omega$  is the apparent rms solid angle of the source:

$$\Omega = 2\pi S'_x S'_y \text{ (mrad}^{\star\star 2}\text{)}$$

and  $S'_{x,y} = \sqrt{\sigma_x'^2 + \lambda/L}$

Here,  $S'_x$  and  $S'_y$  are the apparent divergences of the radiation from the insertion device in the  $x$  and  $y$  directions, and  $\sigma_x'$  and  $\sigma_y'$  are the rms divergences of the electron beam in the  $x$  and  $y$  planes through the insertion device, and  $\lambda$  is the wavelength of the photon beam.

$$\sigma_x' = \sqrt{\epsilon_x / \beta_x}$$

$$\sigma_y' = \sqrt{\epsilon_y / \beta_y}$$

The brilliance is then defined to be:

$$\text{Brilliance} = \frac{\text{number of photons/sec}}{S \times \Omega \text{ (0.1% BW)}}$$

where  $S$  is the rms source area,

$$S = 2\pi S_x S_y$$

$$S_x = \sqrt{\sigma_x^2 + (\lambda L + \sigma_x'^2 L^2)/4}$$

$$S_y = \sqrt{\sigma_y^2 + (\lambda L + \sigma_y'^2 L^2)/4}$$

$$\sigma_x = \sqrt{\beta \epsilon_x}$$

$$\sigma_y = \sqrt{\beta \epsilon_y}$$

#### Undulator Optimization:

Under the given parameters of  $\epsilon_{x0}$ ,  $k$ , and  $\lambda$ , the goal is to obtain the minimum value of  $S \cdot \Omega$  as the function of beta-x and beta-y. In order to demonstrate the sensitivities  $S \cdot \Omega$  which is the four dimensional transverse phase space with respect to the beta functions, we make contour plots of  $1/(S \cdot \Omega)$  as a function of beta-x and beta-y.

Figures 1 - 6 show the inverse of the phase spaces for various photon energies ( $1 \sim 20$  keV). The contours are normalized to the maximum value which is marked with an "H", and each contour line is plotted with an interval of 2% from the previous. In another word, the inner most contour represents 98 percentile and the outer contour represents the 90 percentile contour. Also shown in the figures is the phase space value at the peak in unit of meter squared. The values at null beta functions are calculated at beta = 0.1 m.

Figure 7 shows the result of summing all six contours and renormalized by dividing by 6. This is an attempt to find a universal setting of the beta functions with which all undulator could be efficient.

#### Wiggler Consideration

Detailed consideration of the brightness of wiggler shows that

$$\text{Brightness} = 2N \cdot 3.461 \times 10^6 \gamma^2 I \left(\frac{\epsilon}{\epsilon_c}\right)^2 k_{2/3}^2 \left(\frac{\epsilon}{2\epsilon_c}\right)$$

which is independent of the wiggler geometry. Therefore, to optimize the

brilliance of wiggler, we optimize the quantity S. We have studied this for the photon energies up to 40 keV, and the results are shown in Figure 8. Notice that the brilliance for the wiggler is independent of the photon energy.

#### Conclusion

This simple study shows that for about 5 meter undulator, operating with  $\epsilon_{x0} = \gamma\lambda 10^{-9}$  m and  $k = 0.1$ ,  $\beta_x = 12$  m and  $\beta_y = 6$  m would provide an optimum undulator radiations from 1 - 20 keV range. For wiggler radiation, the beta function setting should be around 2 m for all photon energies.

## UNDULATOR PHASE SPACE CALCULATION

Epsx, Epsy, K2 7.27272727273E-9 7.27272727273E-10 ,1

Photon Wave Length: in Å and in keV 12.397 1

Insertion Device Length 5.2

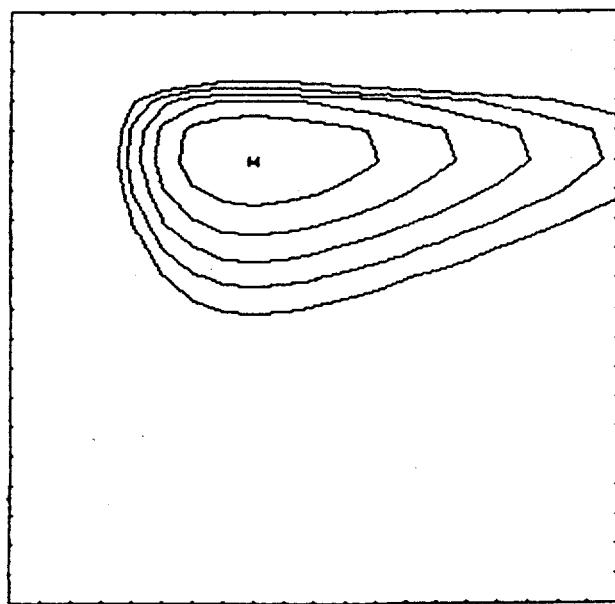
Minimum Value of Phs at Bx By 1.34603E-17 8. 5.

Horizontal Axis Betax: Vertical Axis Betay

Plot is normalized with Phase Space minimum

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
--	---	---	---	---	---	---	---	---	---	---	----	----	----	----	----	----	----	----	----	----	----

0	I	0	4	6	7	7	8	8	8	8	8	8	8	8	8	7	7	7	7	7	
1	I	3	28	44	53	58	60	62	62	62	62	61	61	60	60	59	59	58	57	57	
2	I	4	39	62	74	80	84	86	86	86	86	85	84	83	83	82	81	81	80	79	
3	I	4	43	69	82	90	93	95	96	96	96	95	94	93	92	91	91	90	89	88	
4	I	5	45	71	85	93	97	99	100	100	100	99	98	97	96	95	95	94	93	92	91
5	I	5	45	71	86	93	97	99	100	100	100	99	98	97	96	95	94	93	92	91	91
6	I	5	45	70	85	92	96	98	99	99	99	98	97	96	95	95	94	93	92	91	91
7	I	4	44	69	83	90	94	96	97	97	97	96	95	94	93	92	91	90	89	88	88
8	I	4	43	68	81	88	92	94	95	95	95	94	94	93	92	92	91	90	89	88	87
9	I	4	42	66	79	86	90	92	92	93	92	92	91	91	90	89	89	88	87	86	85
10	I	4	41	64	77	84	88	89	90	90	90	89	88	88	87	87	86	85	84	83	83
11	I	4	40	63	75	82	86	87	88	88	88	88	87	87	86	85	84	84	83	82	81
12	I	4	39	61	74	80	84	85	86	86	86	86	85	84	84	83	82	82	81	80	79
13	I	4	38	60	72	78	82	83	84	84	84	84	83	83	82	81	81	80	79	78	77
14	I	4	37	59	70	77	80	81	82	82	82	81	81	80	79	79	78	77	77	76	75
15	I	4	36	57	69	75	78	80	80	80	80	79	79	78	78	77	76	76	75	74	74
16	I	4	36	56	67	73	76	78	79	79	79	78	78	77	77	76	75	75	74	73	72
17	I	4	35	55	66	72	75	76	77	77	77	76	76	75	74	74	73	73	72	71	71
18	I	3	34	54	65	70	73	75	75	76	75	75	74	74	73	72	72	71	70	70	69
19	I	3	33	53	63	69	72	73	74	74	74	73	73	72	72	71	70	70	69	68	68
20	I	3	33	52	62	68	71	72	73	73	73	72	71	71	70	70	69	68	67	67	67



Array has 21 rows and 21 columns.

Minimum: 59; Maximum: 100; Contour Interval: 2.

Horizontal Axis (right): Betax between 0. 20.

Vertical Axis (down) : Betay between 0. 20.

Figure 1

## UNDULATOR PHASE SPACE CALCULATION

Epsx, Epsy, K2 7.27272727273E-9 7.27272727273E-10 .1

Photon Wave Length: in Å and in keV 2.4794 5

Insertion Device Length 5.2

Minimum Value of Phs at Bx By 7.45302E-18 13. 7.

Horizontal Axis Betax: Vertical Axis Betay

Plot is normalized with Phase Space minimum

		0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
0	I	0	2	3	4	4	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5
1	I	2	20	32	39	43	45	46	47	48	48	48	48	48	48	48	48	48	48	48	48	48
2	I	3	31	50	60	66	70	72	73	74	74	75	75	75	75	75	75	75	75	75	74	74
3	I	4	37	59	71	78	83	85	87	87	88	88	88	88	88	88	88	88	88	88	88	88
4	I	4	39	63	77	85	89	92	93	94	95	95	95	96	96	96	96	95	95	95	95	95
5	I	4	41	65	79	87	92	95	96	97	98	98	99	99	99	99	99	99	99	99	99	99
6	I	4	41	66	80	88	93	96	97	98	98	99	100	100	100	100	100	100	100	100	100	100
7	I	4	41	66	80	88	93	96	97	98	98	99	100	100	100	100	100	100	100	100	100	100
8	I	4	41	66	80	88	92	95	97	98	99	99	99	99	99	99	99	99	99	99	99	99
9	I	4	41	65	79	87	92	94	96	97	98	98	98	98	99	99	99	99	99	99	99	99
10	I	4	40	64	78	86	91	93	95	96	97	97	97	97	97	97	97	97	97	97	97	97
11	I	4	40	64	77	85	89	92	94	95	95	95	96	96	96	96	96	96	96	96	96	96
12	I	4	39	63	76	84	88	91	93	94	94	94	95	95	95	95	95	95	95	95	95	95
13	I	4	39	62	75	83	87	90	91	92	93	93	93	94	94	94	94	94	94	93	93	93
14	I	4	38	61	74	82	86	88	90	91	92	92	92	92	92	92	92	92	92	92	92	92
15	I	4	38	60	73	81	85	87	89	90	90	91	91	91	91	91	91	91	91	91	91	90
16	I	4	37	59	72	79	84	86	88	89	89	90	90	90	90	90	90	90	90	90	89	88
17	I	4	37	59	71	78	83	85	86	87	88	88	89	89	89	89	89	89	88	88	88	88
18	I	4	36	58	70	77	81	84	85	86	87	87	87	88	88	88	87	87	87	87	87	87
19	I	4	36	57	69	76	80	83	84	85	86	86	86	86	86	86	86	86	86	86	86	86
20	I	3	35	56	69	75	79	82	83	84	85	85	85	85	85	85	85	85	85	85	85	85

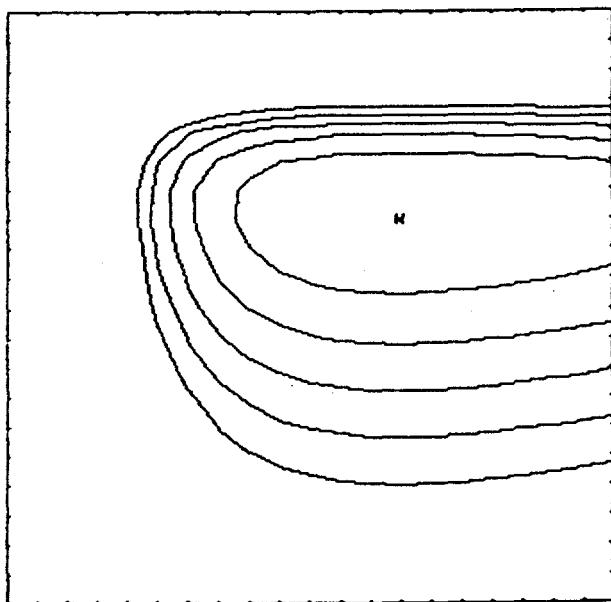
Array has 21 rows and 21 columns.  
Minimum: 0; Maximum: 100; Contour Interval: 2.Horizontal Axis (right): Betax between 0. 20.  
Vertical Axis (down) : Betay between 0. 20.

Figure 2

UNDULATOR PHASE SPACE CALCULATION

Epsx, Epsy, K2    7.27272727273E-9    7.27272727273E-10    .1  
 Photon Wave Length: in Å and in keV    1.2397    10  
 Insertion Device Length    5.2  
 Minimum Value of Phs at Bx By    6.57951E-18    16.    8.

Horizontal Axis Betax: Vertical Axis Betay  
 Plot is normalized with Phase Space minimum

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
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0	I	0	2	3	4	4	4	4	4	4	5	5	5	5	5	5	5	5	5	5
1	I	2	18	29	36	39	41	43	43	44	44	45	45	45	45	45	45	45	45	45
2	I	3	29	46	56	62	65	67	69	70	70	71	71	71	71	71	71	71	71	71
3	I	3	35	56	68	74	78	81	82	83	84	85	85	85	85	86	86	86	86	85
4	I	4	38	60	74	81	85	88	90	91	92	92	93	93	93	93	93	93	93	93
5	I	4	39	63	77	84	89	92	93	95	95	96	97	97	97	97	97	97	97	97
6	I	4	40	64	78	86	91	94	95	97	97	98	98	99	99	99	99	99	99	99
7	I	4	40	65	79	87	92	94	95	97	98	98	99	99	100	100	100	100	100	100
8	I	4	40	65	79	87	92	95	96	98	98	98	99	99	100	100	100	100	100	100
9	I	4	40	65	79	87	92	94	96	97	98	98	99	99	99	100	100	100	100	100
10	I	4	40	65	79	87	91	94	96	97	98	98	99	99	99	99	99	99	99	99
11	I	4	40	64	78	86	91	93	95	96	97	98	98	99	99	99	99	99	99	99
12	I	4	40	64	78	85	90	93	95	96	97	97	98	98	98	98	98	98	98	98
13	I	4	39	63	77	85	89	92	94	95	96	96	97	97	97	97	97	97	97	97
14	I	4	39	63	76	84	89	91	93	94	95	95	96	96	96	97	97	97	97	96
15	I	4	39	62	76	83	88	91	92	93	94	95	95	95	95	96	96	96	96	96
16	I	4	38	62	75	83	87	90	91	93	93	94	94	95	95	95	95	95	95	95
17	I	4	38	61	74	82	86	89	91	92	93	93	94	94	94	94	94	94	94	94
18	I	4	38	61	74	81	86	88	90	91	92	92	93	93	93	93	93	93	93	93
19	I	4	37	60	73	80	85	87	89	90	91	91	92	92	92	92	92	92	92	92
20	I	4	37	60	72	80	84	87	88	89	90	91	91	91	92	92	92	92	92	91

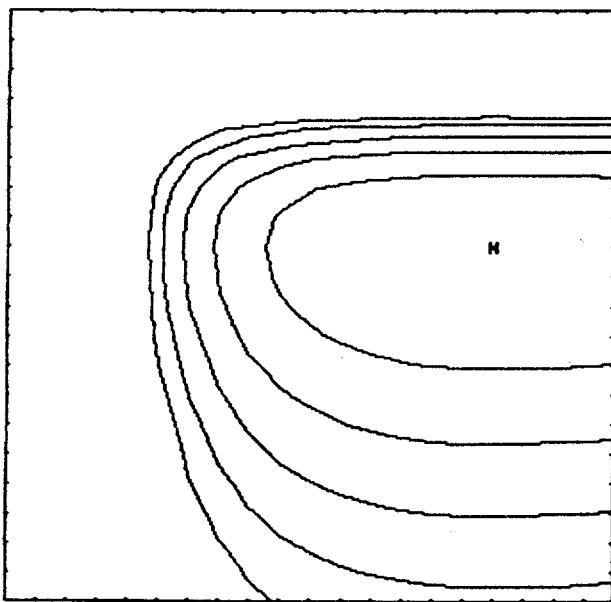


Figure 3

## UNDULATOR PHASE SPACE CALCULATION

Epsx, Epsy, K2 7.27272727273E-9 7.27272727273E-10 .1

Photon Wave Length: in Å and in keV .826466666667 15

Insertion Device Length 5.2

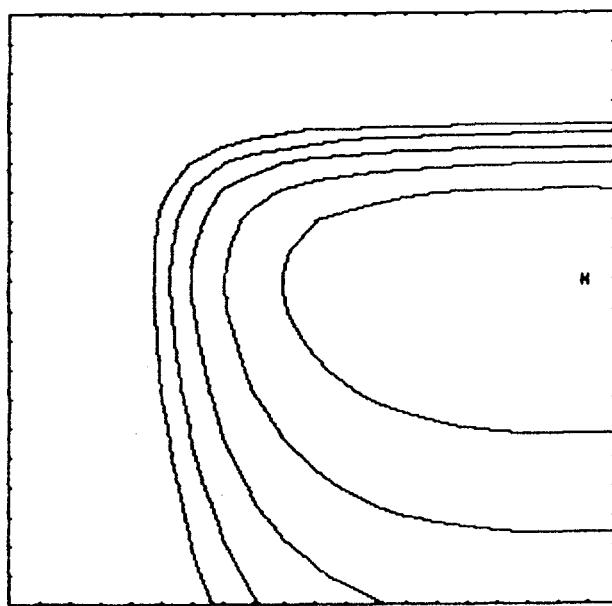
Minimum Value of Phs at Bx By 6.25298E-18 19. 9.

Horizontal Axis Betax; Vertical Axis Betay

Plot is normalized with Phase Space minimum

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
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0	I	0	2	3	3	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4
1	I	2	18	28	34	38	40	41	42	42	43	43	43	43	44	44	44	44	44	44
2	I	3	28	45	55	60	63	65	67	68	68	69	69	69	69	69	69	70	70	70
3	I	3	34	54	66	73	77	79	80	82	82	83	83	83	84	84	84	84	84	84
4	I	4	37	59	72	79	84	86	88	89	90	90	91	91	91	92	92	92	92	92
5	I	4	38	62	75	83	87	90	92	93	94	95	95	95	95	96	96	96	96	96
6	I	4	39	63	77	85	89	92	94	95	96	97	97	98	98	98	98	98	98	98
7	I	4	40	64	78	86	91	93	95	97	97	98	98	98	99	99	99	99	99	99
8	I	4	40	64	78	86	91	94	96	97	98	98	99	99	99	100	100	100	100	100
9	I	4	40	65	79	87	91	94	96	97	98	98	99	99	99	100	100	100	100	100
10	I	4	40	64	78	86	91	94	96	97	98	98	99	99	99	100	100	100	100	100
11	I	4	40	64	78	86	91	94	96	97	98	98	99	99	99	100	100	100	100	100
12	I	4	40	64	78	86	90	93	95	96	97	98	98	99	99	99	99	99	99	99
13	I	4	40	64	78	85	90	93	95	96	97	97	98	98	98	99	99	99	99	99
14	I	4	39	63	77	85	90	92	94	95	96	97	97	98	98	98	98	98	98	98
15	I	4	39	63	77	84	89	92	94	95	96	96	97	97	97	98	98	98	98	98
16	I	4	39	63	76	84	88	91	93	94	95	96	96	96	97	97	97	97	97	97
17	I	4	39	62	76	83	88	91	92	94	94	95	95	96	96	96	96	96	96	96
18	I	4	38	62	75	83	87	90	92	93	94	94	94	95	95	95	95	95	95	95
19	I	4	38	61	75	82	87	89	91	92	93	94	94	94	94	94	94	94	94	94
20	I	4	38	61	74	82	86	89	91	92	93	94	94	94	94	94	94	94	94	94



Minimum: 6.25298E-18 Max: 100.00000E+00, Contour Interval: 2.

Horizontal Axis (right): Betax between 0. 20.  
Vertical Axis (down) : Betay between 0. 20.

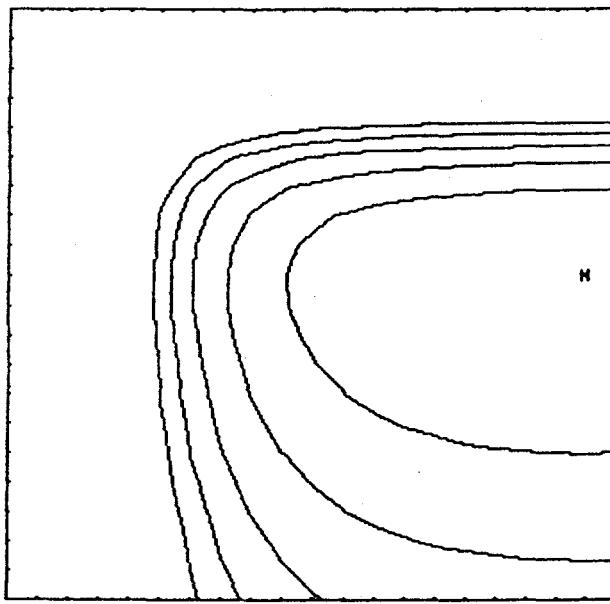
Figure 4

UNDULATOR PHASE SPACE CALCULATION

Epsx, Epsy, K2    7.27272727273E-9    7.27272727273E-10    .1  
 Photon Wave Length: in Å and in keV    .729235294118    17  
 Insertion Device Length    5.2  
 Minimum Value of Phs at Bx By    6.17140E-18    19.    9.

Horizontal Axis Betax: Vertical Axis Betay  
 Plot is normalized with Phase Space minimum

		0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
0	I	0	2	3	3	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4
1	I	2	17	28	34	37	39	41	42	42	42	43	43	43	43	43	43	43	43	43	43	43
2	I	3	28	44	54	60	63	65	66	67	68	68	68	69	69	69	69	69	69	69	69	69
3	I	3	33	54	65	72	76	78	80	81	82	82	83	83	83	83	83	83	83	83	83	83
4	I	4	36	59	72	79	83	86	87	88	89	90	90	91	91	91	91	91	91	91	91	91
5	I	4	38	61	75	83	87	90	92	93	94	94	95	95	95	95	95	95	95	95	95	95
6	I	4	39	63	77	85	88	92	94	95	96	96	97	97	97	98	98	98	98	98	98	98
7	I	4	40	64	78	86	90	93	95	96	97	98	98	98	99	99	99	99	99	99	99	99
8	I	4	40	64	78	86	91	94	96	97	98	98	99	99	99	99	100	100	100	100	100	100
9	I	4	40	64	78	86	91	94	96	97	98	98	99	99	99	99	100	100	100	100	100	100
10	I	4	40	64	78	86	91	94	96	97	98	98	99	99	99	99	100	100	100	100	100	100
11	I	4	40	64	78	86	91	94	96	97	98	98	99	99	99	99	100	100	100	100	100	100
12	I	4	40	64	78	86	91	93	95	96	97	98	98	99	99	99	99	99	99	99	99	99
13	I	4	40	64	78	86	90	93	95	96	97	98	98	99	99	99	99	99	99	99	99	99
14	I	4	39	63	77	85	90	93	94	95	96	96	97	98	98	98	98	98	98	98	98	98
15	I	4	39	63	77	85	88	92	94	95	96	96	97	97	97	98	98	98	98	98	98	98
16	I	4	39	63	76	84	88	92	93	95	95	95	96	97	97	97	97	97	97	97	97	97
17	I	4	39	62	76	84	88	91	93	94	95	95	96	96	96	97	97	97	97	97	97	97
18	I	4	39	62	76	83	88	91	92	94	94	95	95	96	96	96	96	96	96	96	96	96
19	I	4	38	62	75	83	87	90	92	93	94	94	95	95	95	96	96	96	96	96	96	96
20	I	4	38	61	75	82	87	89	91	92	93	94	94	95	95	95	95	95	95	95	95	95



Minimum: 5E-18 Max: 1.0E+00 Contour Interval: 2.  
 Horizontal Axis (right): Betax between 0. 20.  
 Vertical Axis (down) : Betay between 0. 20.

Figure 5

## UNDULATOR PHASE SPACE CALCULATION

Epsx, Epsy, K2    7.27272727273E-9    7.27272727273E-10    .1  
 Photon Wave Length: in Å and in keV    .61985    20  
 Insertion Device Length    5.2  
 Minimum Value of Phs at Bx By    6.07539E-18    20.    10.

Horizontal Axis Betax: Vertical Axis Betay  
 Plot is normalized with Phase Space minimum

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
0	I	0	2	3	3	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4	4
1	I	2	17	28	34	37	39	40	41	42	42	42	42	43	43	43	43	43	43	43	43
2	I	3	27	44	54	59	62	64	66	66	67	67	68	68	68	68	68	68	68	69	69
3	I	3	33	53	65	71	75	78	79	80	81	82	82	82	83	83	83	83	83	83	83
4	I	4	36	58	71	78	82	85	87	88	88	89	90	90	90	91	91	91	91	91	91
5	I	4	38	61	74	82	86	89	91	92	93	94	94	94	95	95	95	95	95	95	95
6	I	4	39	63	76	84	89	91	93	95	95	95	96	97	97	97	97	97	98	98	98
7	I	4	39	64	77	85	90	93	95	96	97	97	98	98	98	99	99	99	99	99	99
8	I	4	40	64	78	86	91	93	95	97	97	98	98	98	99	99	99	99	100	100	100
9	I	4	40	64	78	86	91	94	96	97	98	98	99	99	99	100	100	100	100	100	100
10	I	4	40	64	78	86	91	94	96	97	98	98	99	99	99	100	100	100	100	100	100
11	I	4	40	64	78	86	91	94	96	97	98	98	99	99	99	100	100	100	100	100	100
12	I	4	40	64	78	86	91	93	95	97	97	98	98	99	99	99	99	99	100	100	100
13	I	4	40	64	78	86	90	93	95	96	97	98	98	99	99	99	99	99	99	99	99
14	I	4	39	64	77	85	90	93	95	96	97	97	98	98	98	99	99	99	99	99	99
15	I	4	39	63	77	85	90	92	94	95	96	97	97	98	98	98	98	98	98	98	98
16	I	4	39	63	77	85	89	92	94	95	96	97	97	97	98	98	98	98	98	98	98
17	I	4	39	63	75	84	89	92	93	95	95	96	96	97	97	97	97	98	98	98	98
18	I	4	39	62	76	84	88	91	93	94	95	96	96	96	97	97	97	97	97	97	97
19	I	4	39	62	76	83	88	91	92	94	94	95	95	96	96	96	96	96	97	97	97
20	I	4	38	62	75	83	87	90	92	93	94	95	95	95	96	96	96	96	96	96	96

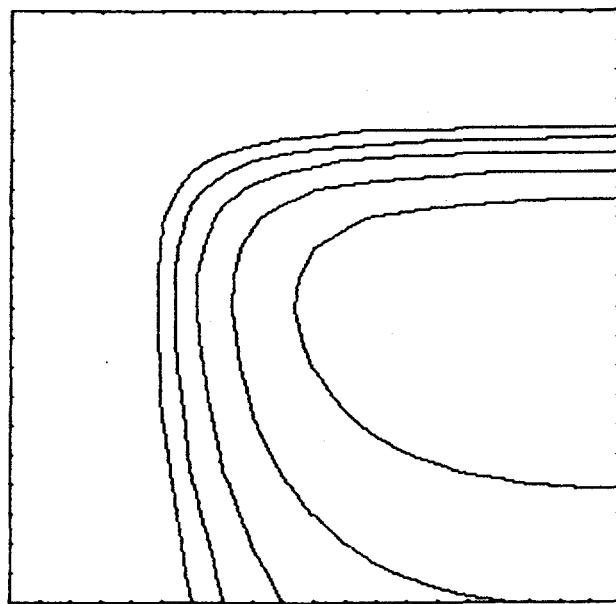
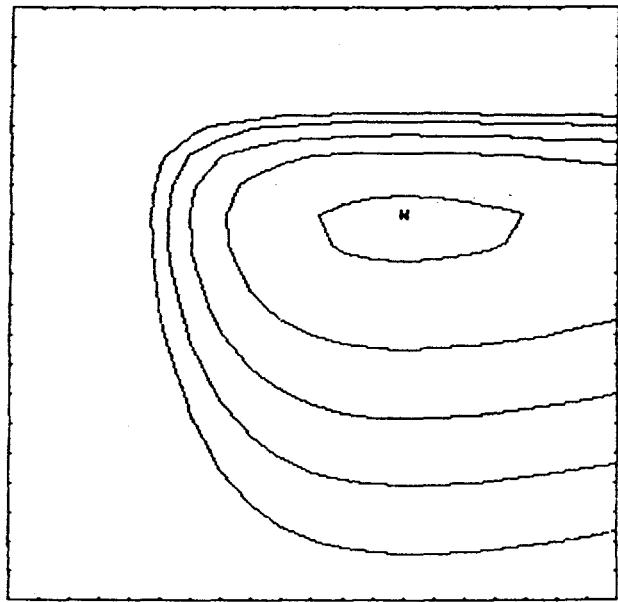


Figure 6

Horizontal Axis (right): Betax between 0. 20.  
 Vertical Axis (down) : Betay between 0. 20.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
0	I	0	2	3	4	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5	5
1	I	2	20	32	38	42	44	45	46	47	47	47	47	47	47	47	47	47	47	47	47
2	I	3	30	48	59	65	68	70	71	72	72	73	73	73	73	73	72	72	72	72	72
3	I	4	36	57	70	76	80	83	84	85	86	86	86	86	86	86	86	86	86	85	85
4	I	4	39	62	75	82	87	89	91	92	92	93	93	93	93	93	93	93	92	92	92
5	I	4	40	64	78	85	90	92	94	95	96	96	96	96	96	96	96	96	96	95	95
6	I	4	41	65	79	87	91	94	95	96	97	97	98	98	98	98	98	98	97	97	97
7	I	4	41	65	79	87	92	94	96	97	98	98	98	98	98	98	98	98	98	98	97
8	I	4	41	65	79	87	91	94	96	97	97	98	98	98	98	98	98	98	98	98	97
9	I	4	40	65	79	87	91	94	95	95	96	97	97	98	98	98	98	98	97	97	97
10	I	4	40	64	78	86	90	93	95	96	96	97	97	97	97	97	97	97	97	97	96
11	I	4	40	64	78	85	90	92	94	95	96	96	96	96	96	96	96	96	96	96	96
12	I	4	39	63	77	85	89	92	93	94	95	95	95	96	96	96	96	95	95	95	95
13	I	4	39	63	76	84	88	91	92	93	94	94	95	95	95	95	95	94	94	94	94
14	I	4	39	62	75	83	87	90	91	92	93	93	94	94	94	94	94	94	93	93	93
15	I	4	38	62	75	82	86	89	91	92	92	93	93	93	93	93	93	93	92	92	92
16	I	4	38	61	74	81	86	88	90	91	91	92	92	92	92	92	92	92	92	91	91
17	I	4	38	60	73	81	85	87	89	90	90	91	91	91	91	91	91	91	91	91	90
18	I	4	37	60	73	80	84	86	88	89	90	90	90	90	90	90	90	90	90	90	90
19	I	4	37	59	72	79	83	86	87	88	89	89	89	89	89	89	89	89	89	89	89
20	I	4	37	59	71	78	82	85	86	87	88	88	89	89	89	89	89	89	89	89	89



Array has 21 rows and 21 columns.  
Minimum: 50; Maximum: 100; Contour Interval: 2.

Figure 7. Summed Contour Plot of Fig. 1-6.

WIGGLER RADIATION PHASE SPACE CALCULATION

Epsx, Epsy, K2 7.27272727273E-9 7.27272727273E-10 .1

Photon Wave Length: in Å and in keV .309925 40

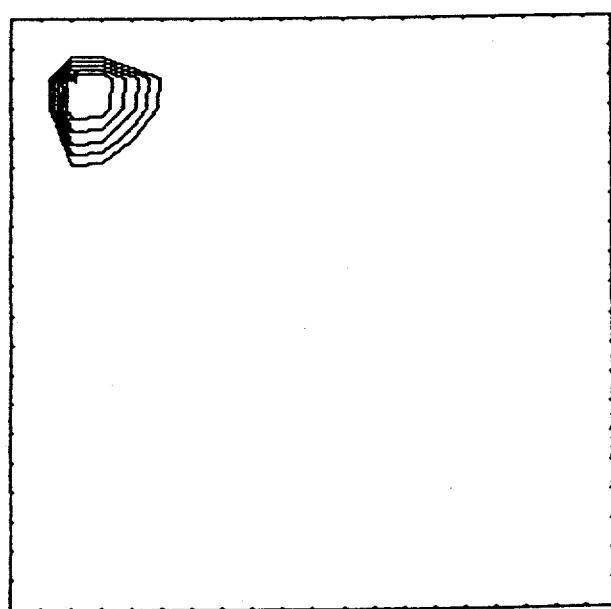
Insertion Device Length 5

Minnimum Value of Phs at Bx By 1.17417E-08 2. 2.

Horizontal Axis Betax: Vertical Axis Betay

Plot is normalized with Phase Space minimum

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	
0	I	8	25	29	29	27	26	24	23	22	21	20	19	18	18	17	16	16	15	15	14	
1	I	25	75	87	86	82	78	73	69	66	62	60	57	55	53	51	50	48	47	45	44	43
2	I	28	87	100	100	95	90	84	80	76	72	69	66	63	61	59	57	56	54	52	51	50
3	I	28	86	100	99	95	89	84	79	75	72	69	66	63	61	59	57	55	54	52	51	50
4	I	27	82	95	95	90	85	80	76	72	68	65	63	60	58	56	54	53	51	50	49	47
5	I	26	78	90	89	85	80	76	72	68	65	62	60	57	55	53	51	50	48	47	46	45
6	I	24	73	85	84	80	76	71	67	64	61	58	56	54	52	50	48	47	46	44	43	42
7	I	23	68	80	80	76	72	67	64	60	58	55	53	51	49	47	46	44	43	42	41	40
8	I	22	66	76	76	72	68	64	60	57	55	52	50	48	46	45	43	42	41	40	39	38
9	I	21	62	72	72	69	65	61	58	55	52	50	48	46	44	43	41	40	39	38	37	36
10	I	20	60	69	69	66	62	58	55	52	50	48	46	44	42	40	39	38	37	36	35	34
11	I	19	57	66	66	63	59	56	53	50	48	46	44	42	40	39	38	36	35	34	33	32
12	I	18	55	64	63	60	57	54	51	48	46	44	42	40	39	38	36	35	34	33	32	31
13	I	17	53	61	61	58	55	52	49	46	44	42	40	39	38	36	35	34	33	32	31	30
14	I	17	51	59	59	56	53	50	47	45	43	41	39	38	36	35	34	33	32	31	30	29
15	I	16	50	57	57	55	51	48	46	43	41	39	37	35	34	33	32	31	30	29	28	27
16	I	16	48	56	55	53	50	47	44	42	40	38	37	35	34	33	32	31	30	29	28	27
17	I	15	47	54	54	51	48	46	43	41	39	37	35	34	33	32	31	30	29	28	27	26
18	I	15	46	53	52	50	47	44	42	40	38	36	35	34	33	32	31	30	29	28	27	26
19	I	15	44	51	51	49	46	43	41	39	37	35	34	33	32	31	30	29	28	27	26	25
20	I	14	43	50	50	48	45	42	40	38	36	34	33	32	31	30	29	28	27	26	25	25



Minimum: 88; Maximum: 701; Total: 21 rows and 21 columns.

Horizontal Axis (right): Betax between 0. 20.

Vertical Axis (down) : Betay between 0. 20.

Figure 8