

PHYSICS GROUP V

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from here NCC  
O.P. 13

Metal Testing

Calibration -  $\frac{\Delta k}{\Delta ih}$

The critical positions of the control rod were determined with and without 29.7 grams of iron wire wrapped around each of the 16 eggs in Lot #1. The results of the measurements follow:

No iron	Critical position	126.29 ih
With iron	" "	<u>121.80</u>
	$\Delta ih$ due to iron poisoning	4.49 ih

The percent change in reproduction factor per cell caused by the introduction of the iron poisoning can be calculated from the following formula:

$$\Delta k\% = 100 \frac{a}{b} D \times f \times \frac{W_i}{W_u}$$

where  $\frac{a}{b}$  is the ratio of neutron density at the surface of the metal lump (where the iron was placed) to the average neutron density inside the lumps; D is the danger coefficient of iron, f is the thermal utilization of the cell,  $W_i$  is the average weight of iron per cell, and  $W_u$  the average weight of the uranium per cell.

The ratio  $\frac{a}{b}$  can be calculated for an equivalent spherical lump (radius = 2.94 cm) assuming a neutron density variation inside the lump of the form:

$$\frac{\sinh kr}{r}$$

The ratio  $\frac{a}{b}$  is then given by the following expression:

$$\frac{a}{b} = \frac{\int_0^R \sinh(kr) dr}{R \sinh(kR)} = \frac{(kR)^2 \sinh(kR)}{3[kR \cosh(kR) - \sinh(kR)]}$$

Using Mr. Wigner's value of k for metal of density 18.8 gms/cm<sup>3</sup>

$$k = .0424 \times 18.8 = .796$$

and with R = 2.94 cm

We obtain  $\frac{a}{b} = 1.32$

with D = 1.32 from measurements with CP #1  
f = .83

$W_i = 29.7$   
 $W_u = 1987$